

Homework Assignment No. 11 Solutions

Problem 1 – (10 points)

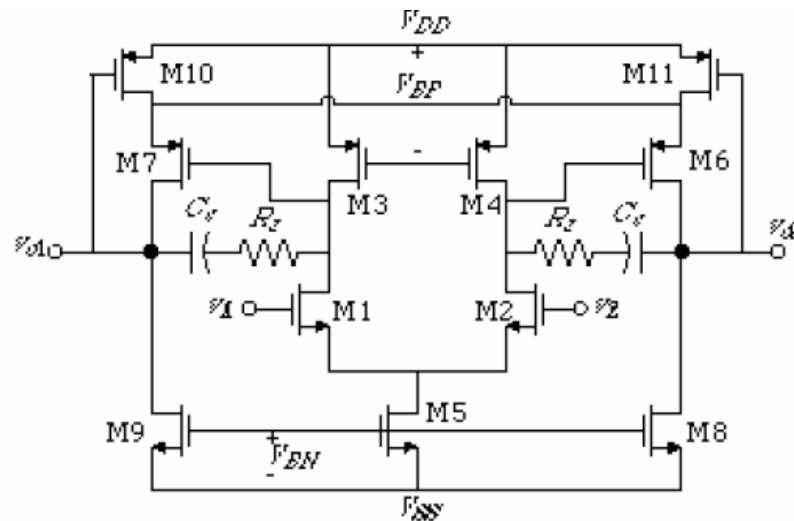


Figure 7.3-12 Two-stage, Miller, differential-in, differential-out op amp with common-mode stabilization.

The loop gain of the common-mode feedback loop is,

$$\text{CMFB Loop gain} \approx -\frac{g_{m10}}{g_{ds9}} = -g_{m10}r_{ds9} \quad \text{or} \quad -\frac{g_{m11}}{g_{ds8}} = -g_{m11}r_{ds8}$$

With $I_D = 50\mu\text{A}$ and $W/L = 10\mu\text{m}/1\mu\text{m}$, $g_{m10} = \sqrt{\frac{2K_P'WI_D}{L}} = \sqrt{2 \cdot 50 \cdot 10 \cdot 50} = 223.6\mu\text{S}$,

$$r_{dsN} = \frac{1}{\lambda_N I_D} = \frac{25}{50\mu\text{A}} = 0.5\text{M}\Omega \quad \text{and} \quad r_{dsP} = \frac{1}{\lambda_P I_D} = \frac{20}{50\mu\text{A}} = 0.4\text{M}\Omega$$

$$\therefore \boxed{\text{CMFB Loop gain} \approx -g_{m10}r_{ds9} = -223.6(0.5) = -111.8\text{V/V}}$$

If the output is cascoded, the gain becomes,

$$\begin{aligned} \text{CMFB Loop gain with cascoding} &\approx -\frac{g_{m10}}{g_{ds9}} g_m(\text{cascode})r_{ds}(\text{cascode}) \\ &= -g_{m10}\{[r_{ds9} g_m(\text{cascode})r_{ds}(\text{cascode})]\| [g_{m7}r_{ds7} (r_{ds10}\|r_{ds10})]\} \end{aligned}$$

$$g_{mP} = \sqrt{\frac{2K_N'WI_D}{L}} = \sqrt{2 \cdot 110 \cdot 10 \cdot 50} = 331.67\mu\text{S}$$

$$= -(223.6)[(0.5 \cdot 331.67 \cdot 0.5)\|(223.6)(0.4)(0.2)] = 223.6(14.7) = -3,290\text{ V/V}$$

$$\therefore \boxed{\text{CMFB Loop gain with cascoding} \approx -3.290\text{V/V}}$$

Problem 2 – (10 points)

Common mode half circuit:

$$V_{o1} = V_{o2} = V_{DD} - |V_{GS3}|$$

$$|V_{GS3}| = \sqrt{\frac{2I_D}{k_p \cdot \frac{w}{L}}} + V_{TP} = |V_{ov}| + V_{TP} = 0.8V$$

$$\Rightarrow V_{o1} = V_{o2} = 2.5 - 0.8 = 1.7V$$

$$a_{dm} = -g_{m1}(r_{o1} \parallel r_{o3} \parallel 20K) = -1(100 \parallel 200 \parallel 20) = -15.38, \text{ where}$$

$$g_{m1} = \sqrt{2k_n \cdot \frac{w}{L} I_D} = k_n \cdot \frac{w}{L} v_{ov} = 5000 \times 0.2 = 1mS$$

$$v_{ov} = \frac{\sqrt{2I_{D3}}}{\sqrt{k_p \cdot \left(\frac{w}{L}\right)_3}} \Rightarrow 0.2 = \frac{\sqrt{2 \times 100\mu}}{\sqrt{k_p \cdot \left(\frac{w}{L}\right)_3}} \Rightarrow \begin{cases} k_p \cdot \left(\frac{w}{L}\right)_3 = 5000\mu \\ k_n \cdot \left(\frac{w}{L}\right)_1 = 5000\mu \end{cases}$$

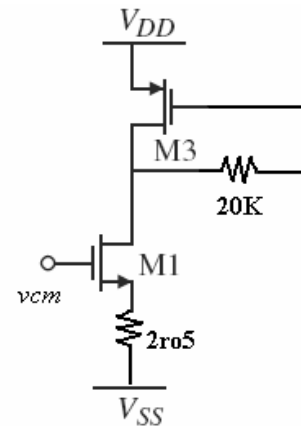
$$r_{o1} = 100K, r_{o3} = 200K$$

$$a_{cm} = -\frac{g_{m1}}{1 + 2g_{m1}r_{o5}} (r_{o1}(1 + 2g_{m1}r_{o5}) \parallel r_{o3} \parallel \frac{1}{g_{m3}}) = \frac{1}{1 + 2m \times 50K} = 0.01, \text{ where:}$$

$$g_{m3} = 5000 \times 0.2 = 1mS$$

$$r_{o5} = 50K$$

Because of adding the 20K resistors, the a_{dm} becomes smaller but a_{cm} becomes much smaller. The effective impedance of M_3 and M_4 is now $1/g_m$, which is much smaller than $r_o \rightarrow a_{dm}/a_{cm} = 1538$ which is much higher than 100 in 12.4.1



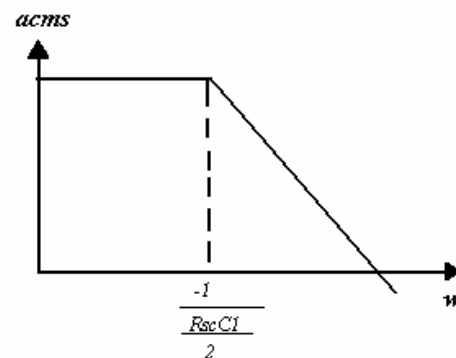
Problem 3 – (10 points)

Without C_{cs} :

$$v_{cms} = (v_{ov1} + v_{ov2}) \frac{(R_{cs} \parallel \frac{1}{C_1s})}{(R_{cs} \parallel \frac{1}{C_1s}) + R_{cs}}$$

$$v_{oc} = \frac{v_{ov1} + v_{ov2}}{2}$$

$$\frac{v_{cms}}{v_{oc}} = 2 \frac{R_{cs}}{R_{cs} + R_{cs}(R_{cs}C_1s + 1)} \Rightarrow a_{cms} = \frac{1}{1 + \frac{R_{cs}C_1s}{2}}$$



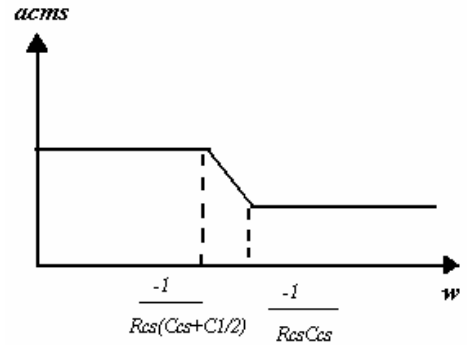
Gain starts to drop at frequencies higher than the pole. In Other words the CM detector cannot follow the signal at the same rate.

With C_{cs} :

$$v_{cms} = (v_{ov1} + v_{ov2}) \frac{(R_{cs} \parallel \frac{1}{(C_{cs} + C_1)s})}{(R_{cs} \parallel \frac{1}{(C_{cs} + C_1)s}) + (R_{cs} \parallel \frac{1}{C_{cs}s})}$$

$$v_{oc} = \frac{v_{ov1} + v_{ov2}}{2}$$

$$\frac{v_{cms}}{v_{oc}} = 2 \frac{R_{cs} C_{cs} s + 1}{R_{cs} C_{cs} s + 1 + 1 + R_{cs} (C_1 s + C_{cs} s)} \Rightarrow a_{cms} = \frac{1 + R_{cs} C_{cs} s}{1 + R_{cs} (C_{cs} + \frac{C_1}{2}) s}$$



If $C_{cs} \gg \frac{C_1}{2} \rightarrow$ gain stays constant over the entire frequency range.

Problem 4 – (10 points)

$$\frac{(\frac{w}{L})_{12}}{(\frac{w}{L})_{11}} = \frac{20}{100} \Rightarrow (\frac{w}{L})_{12} = 19.2 \Rightarrow w_{12} = 19.2 \mu m$$

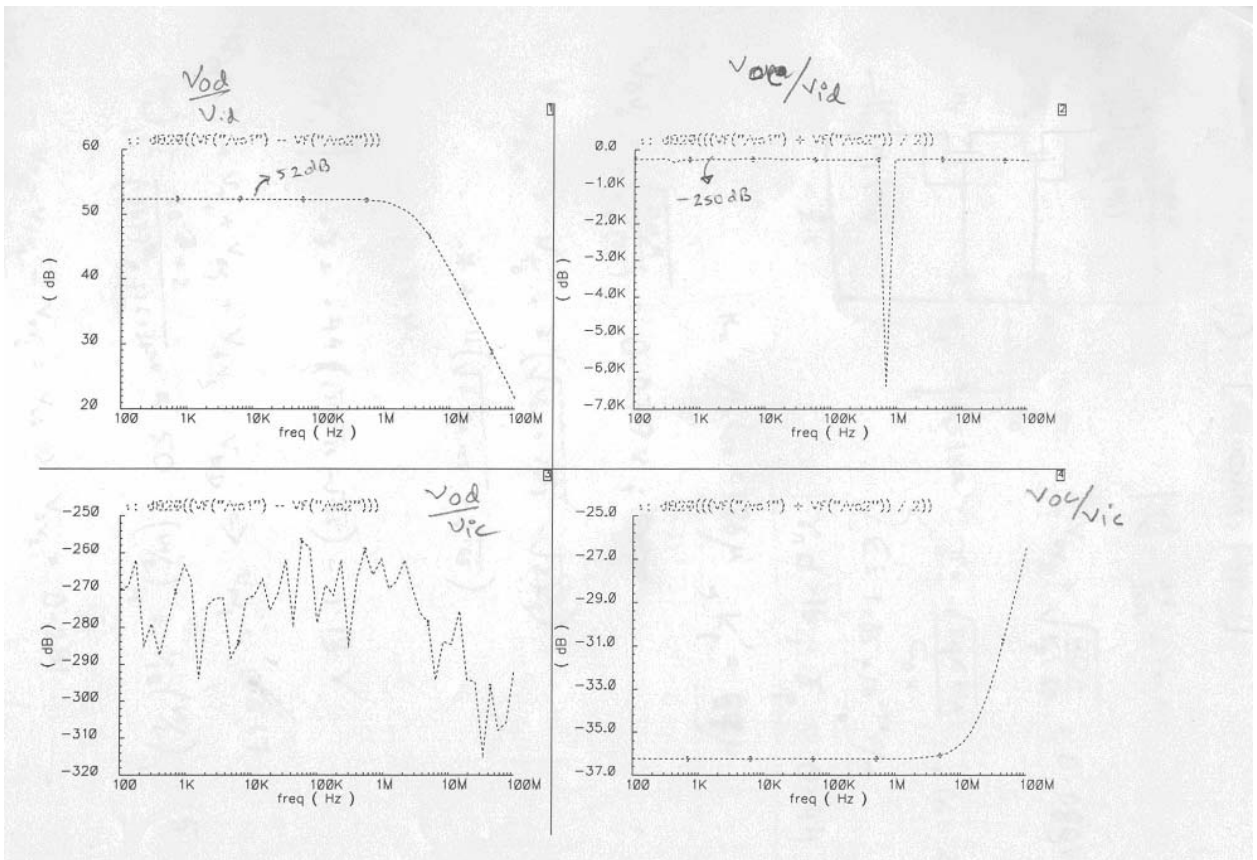
$$I_{D51} = 120 \mu$$

$$\frac{(\frac{w}{L})_{51}}{(\frac{w}{L})_{14}} = \frac{120}{100} \Rightarrow (\frac{w}{L})_{51} = 1.2 \times \frac{16}{0.8} \times 0.8 = 19.2 \Rightarrow w_{51} = 19.2 \mu m$$

$$SR = \frac{100 \mu A}{4 pF} = 25 V / \mu sec$$

$$v_{o1 \min} = \max(-1.65 + v_{ov51} + v_{ov1} + v_{ov1C}, v_i - v_t + v_{ov1C})$$

$$v_{o1 \max} = 1.65 - v_{ov27} - v_{gs24}$$



Problem 5 – (10 points)

$$v_o^+ = v_{DD} - v_{ds3} - v_{gs1}$$

$$v_o^- = v_{DD} - v_{ds6} - v_{gs2}$$

$$k_n' = \mu_n C_{ox} = 126, k_p' = \mu_p C_{ox} = 57$$

$$v_{ov6} = \sqrt{\frac{20\mu}{k_n'(25)}} = 0.079V$$

$$v_{ov3} = \sqrt{\frac{20\mu}{k_p'(50)}} = 0.083V$$

$$V_m = V_{t0} + 0.16(\sqrt{3.5+0.65} - \sqrt{0.65}) = 0.897V$$

$$\Rightarrow v_{gs1} = 2.5 - 1 - 0.083 = 1.41V$$

$$\Rightarrow \left(\frac{w}{L}\right)_1 = \frac{2 \times 1mA}{126\mu \times (1.41 - 0.897)^2} = 60, \left(\frac{w}{L}\right)_4 = 0.1 \times 60 = 6$$

$$V_{tp} = V_{t0} - 0.44(\sqrt{3.5+0.65} - \sqrt{0.65}) = -1.242V$$

$$\Rightarrow v_{gs2} = -2.5 + 1 + 0.079 = 1.421V$$

$$\Rightarrow \left(\frac{w}{L}\right)_2 = \frac{2 \times 1mA}{57\mu \times (1.421 - 1.242)^2} = 1095, \left(\frac{w}{L}\right)_4 = 0.1 \times 1095 = 109.5$$

