

### Logic Simplification and Design

Consider the logical function:

$$Out = \overline{(\overline{A + B}) + B} \overline{D} + \overline{(\overline{C} + B)(A + D)(\overline{B} + \overline{C} + \overline{D})}$$

**Part A** Implement the function using 2-input and 3-input NAND gates and inverters. Use a MIXED LOGIC design methodology. All bubbles must be paired; all bars must be bubbled.

**Part B** Use DeMorgan's Theorem to obtain an equivalent expression which contains ANDs and ORs of the inputs (e.g.,  $A$ ) and their complements (e.g.,  $\overline{A}$ ). There should be **no complements (bars)** in the final expression except those over the inputs. Do **not** simplify the expression for this part.

$Out =$

**Part C** Complete the Karnaugh map below and identify the prime implicants. Then write the simplified expression. Be sure to factor out any common terms in your solution.

	$\overline{B}$	$B$			
	⏟		⏟		
$\overline{A}$					$\overline{C}$
	⏟		⏟		
$A$					$C$
	⏟		⏟		
$A$					$\overline{C}$
	⏟		⏟		
	$\overline{D}$	$D$	$\overline{D}$		
	⏟		⏟		

  

	prime implicant	essential?
_____		yes <input type="checkbox"/> no <input type="checkbox"/>
_____		yes <input type="checkbox"/> no <input type="checkbox"/>
_____		yes <input type="checkbox"/> no <input type="checkbox"/>
_____		yes <input type="checkbox"/> no <input type="checkbox"/>
_____		yes <input type="checkbox"/> no <input type="checkbox"/>
_____		yes <input type="checkbox"/> no <input type="checkbox"/>
_____		yes <input type="checkbox"/> no <input type="checkbox"/>

*Out* = \_\_\_\_\_

**Part D** Now reimplement the simplified expression from part C using 2-input NAND gates and inverters. Use the MIXED LOGIC design methodology. All bubbles must be paired; all bars must be bubbled.