$\qquad$

## HW-7. Finite State Machine - Circuit Design

Design the logic to implement the following FSM. This is the state diagram for a Mealy machine with 3 states that outputs a " 1 " on every third " 1 " received as input, no matter how many " 0 "s are intermingled. For example:

Input: 010110100101110110110
Output: $0000 \overline{1} 000000 \overline{1} 000 \overline{1} 000 \overline{10} 0$


This is the truth table for the logic that is needed. $\mathrm{P} 1, \mathrm{P} 0$ is the present state, Number the states such that $2 * \mathrm{P} 1+\mathrm{P} 0$ is the number of 1's seen in the present sequence of 3 . N1,N0 the next state.

| P1 | P0 | Input | N1 | N0 | Output |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ |
| 0 | 0 | 1 | $\mathbf{0}$ | $\mathbf{1}$ | $\mathbf{0}$ |
| 0 | 1 | 0 | $\mathbf{0}$ | $\mathbf{1}$ | $\mathbf{0}$ |
| 0 | 1 | 1 | $\mathbf{1}$ | $\mathbf{0}$ | $\mathbf{0}$ |
| 1 | 0 | 0 | $\mathbf{1}$ | $\mathbf{0}$ | $\mathbf{0}$ |
| 1 | 0 | 1 | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{1}$ |

Answer $\qquad$
$\mathrm{N} 1=\mathrm{P} 1 \cdot \mathrm{I}^{\prime}+\mathrm{P} 0 \cdot \mathrm{I}$

| Input (I) - P1,P0 | 00 | 01 | 11 | 10 |
| :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | x | 1 |
| 1 | 0 | 1 | x | 0 |

$\mathrm{N} 0=\mathrm{P} 0 \bullet \mathrm{I}^{\prime}+\mathrm{P} 1^{\prime} \bullet \mathrm{P} 0^{\prime} \bullet \mathrm{I}$

| Input (I) - P1,P0 | 00 | 01 | 11 | 10 |
| :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 1 | x | 0 |
| 1 | 1 |  | 0 | x |

Output $=\mathrm{P} 1 \bullet \mathrm{P} 0^{\prime} \bullet \mathrm{I}$

| Input (I) - P1,P0 | 00 | 01 | 11 | 10 |
| :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | x | 0 |
| 1 | 0 | 0 | x | 1 |

$\qquad$

$$
\begin{aligned}
& \mathrm{N} 1=\mathrm{P} 1 \bullet \mathrm{I}^{\prime}+\mathrm{P} 0 \bullet \mathrm{I} \\
& \mathrm{~N} 0=\mathrm{P} 0 \cdot \mathrm{I}^{\prime}+\mathrm{P} 1^{\prime} \cdot \mathrm{P} 0^{\prime} \cdot \mathrm{I} \\
& \text { Output }=\mathrm{P} 1 \cdot \mathrm{P} 0^{\prime} \cdot \mathrm{I}
\end{aligned}
$$



Not-Connected Lines


Connected Lines

